

LECTURE

01

प्रांस
BATCH

CLASS XI - PHYSICS

MOTION IN A STRAIGHT LINE



Next
Toppers



Yaad h ye sab?



- Mechanics
- Frame of Reference
- Rest and Motion
- Distance and Displacement
- Average Speed and Velocity
- Uniform Speed and Non-Uniform Speed
- Uniform Velocity and Non-Uniform Velocity

Mechanics deals with the motion of objects and it can be divided into two branches:

Kinematics



- Study of motion without considering the causes behind it.
- It explores how objects move, not why they move.

Dynamics



- Study of motion, along with the forces and reasons that cause it.
- It explains why objects move the way they do.

Examples of motion studied in Kinematics:

- ✓ Motion along a straight line (1D motion)
- ✓ Motion in a plane (2D motion)
- ✓ Circular motion

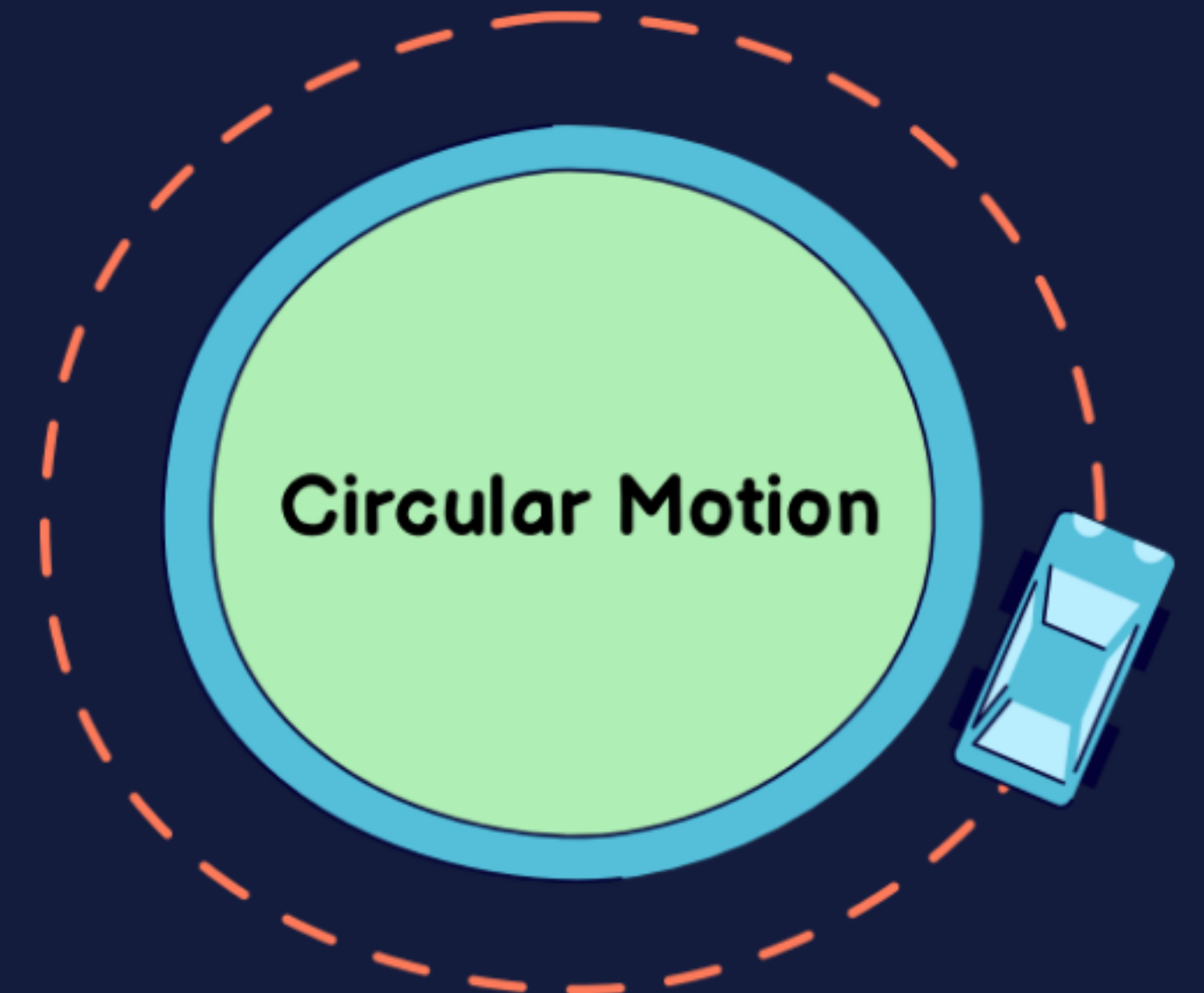
1-D Motion



2-D Motion



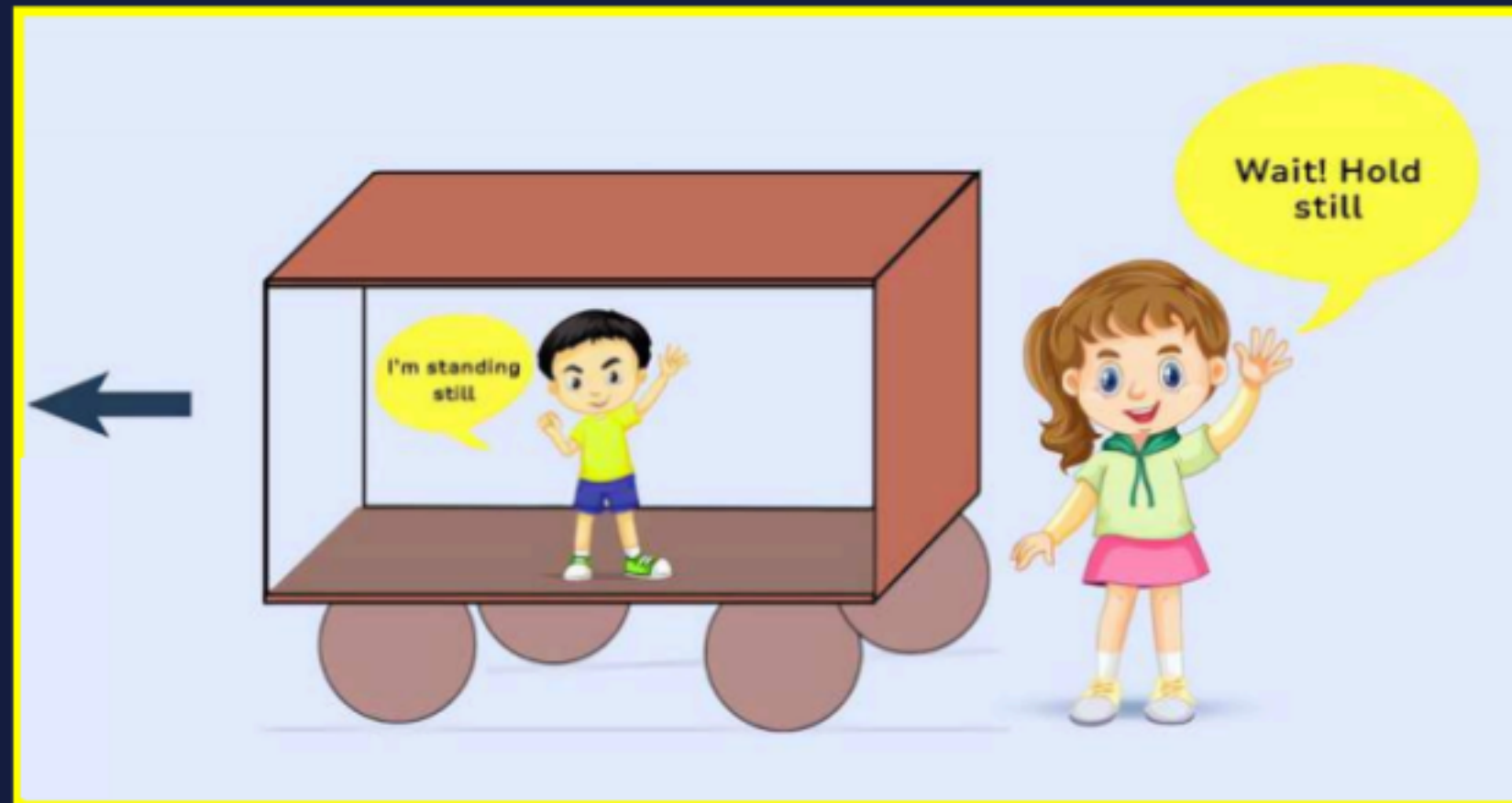
Circular Motion



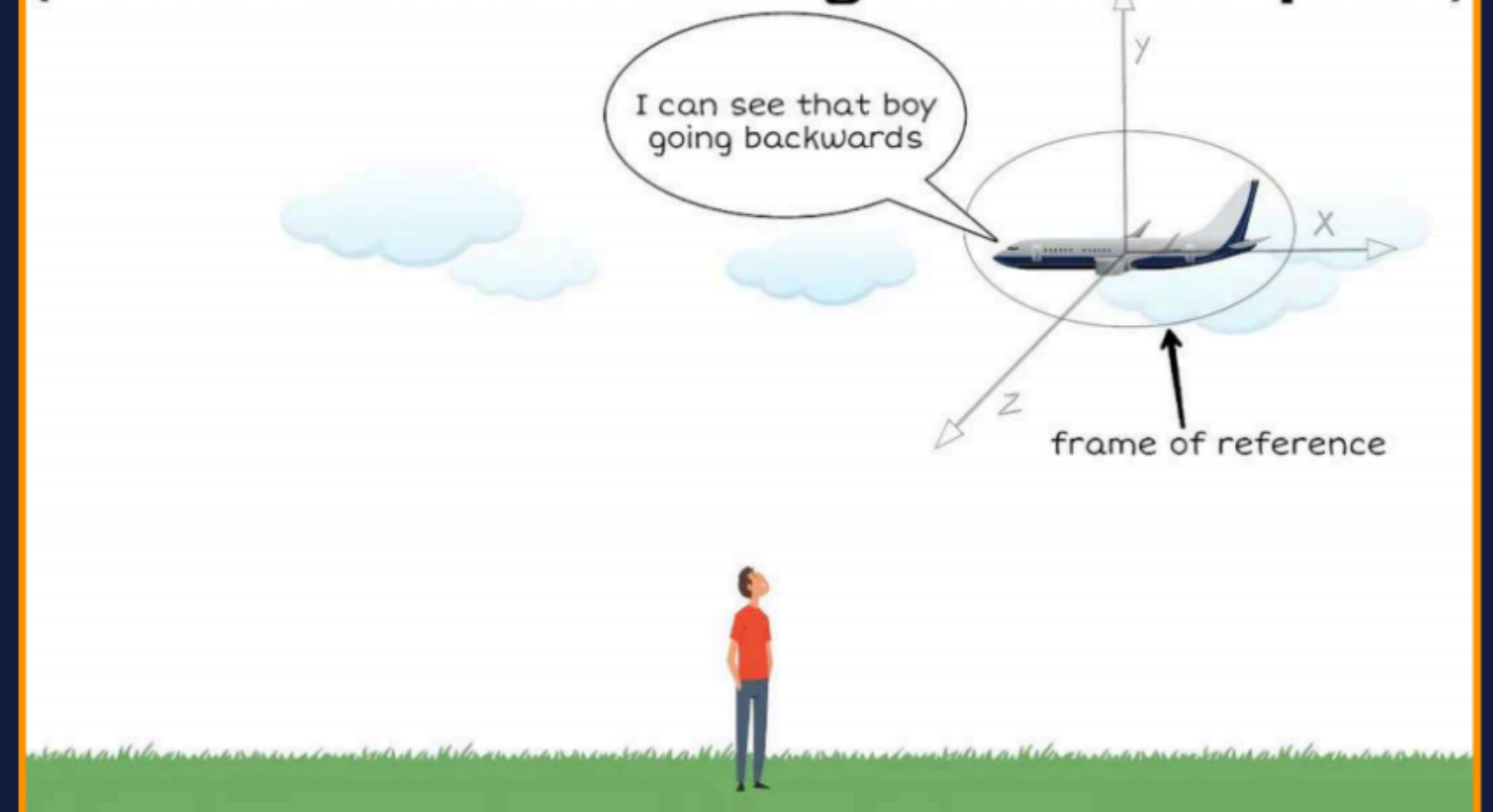
Frame of Reference

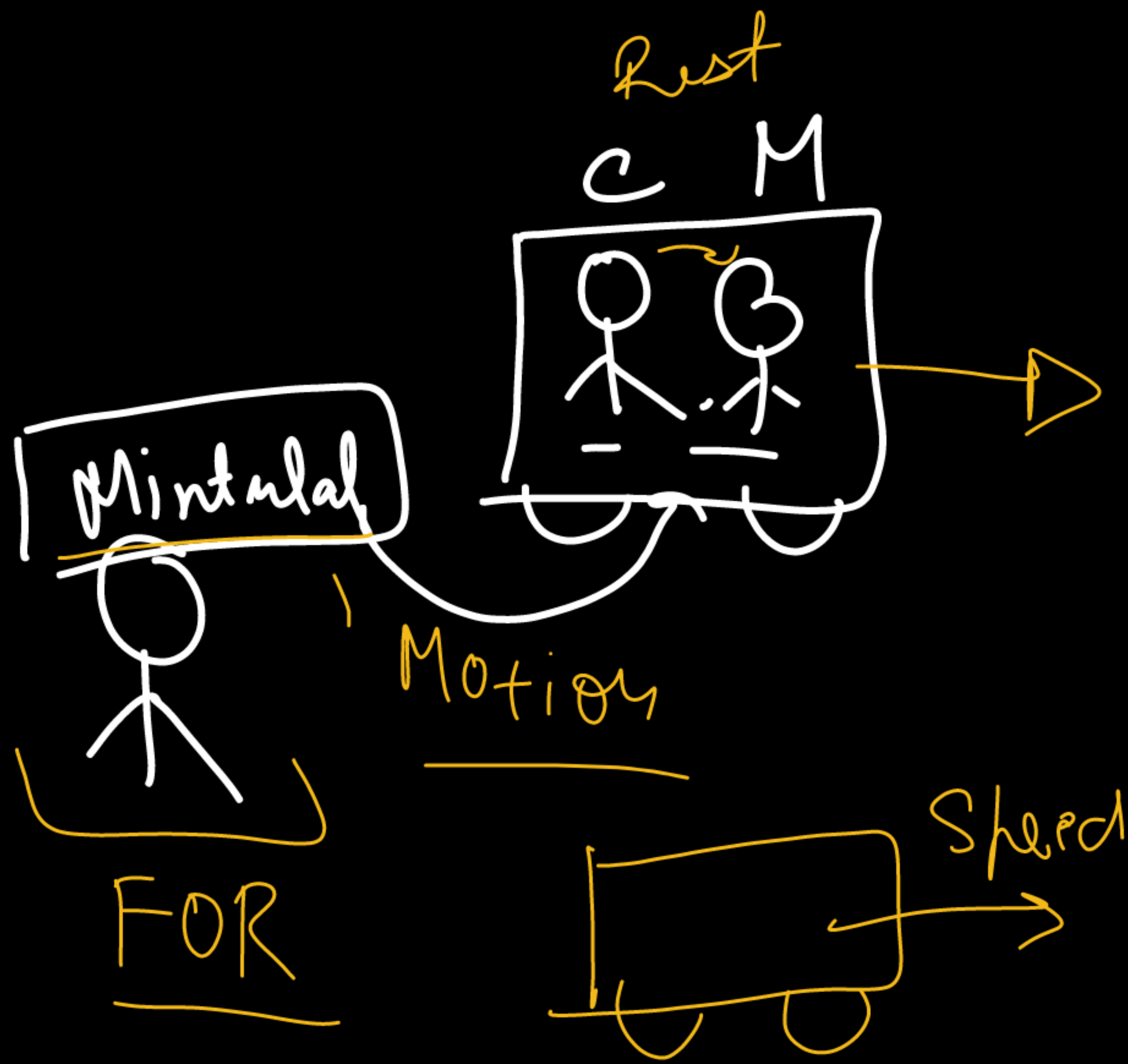
A frame of reference is a system used to describe the position, velocity, and motion of objects.

Everything depends on where you stand!

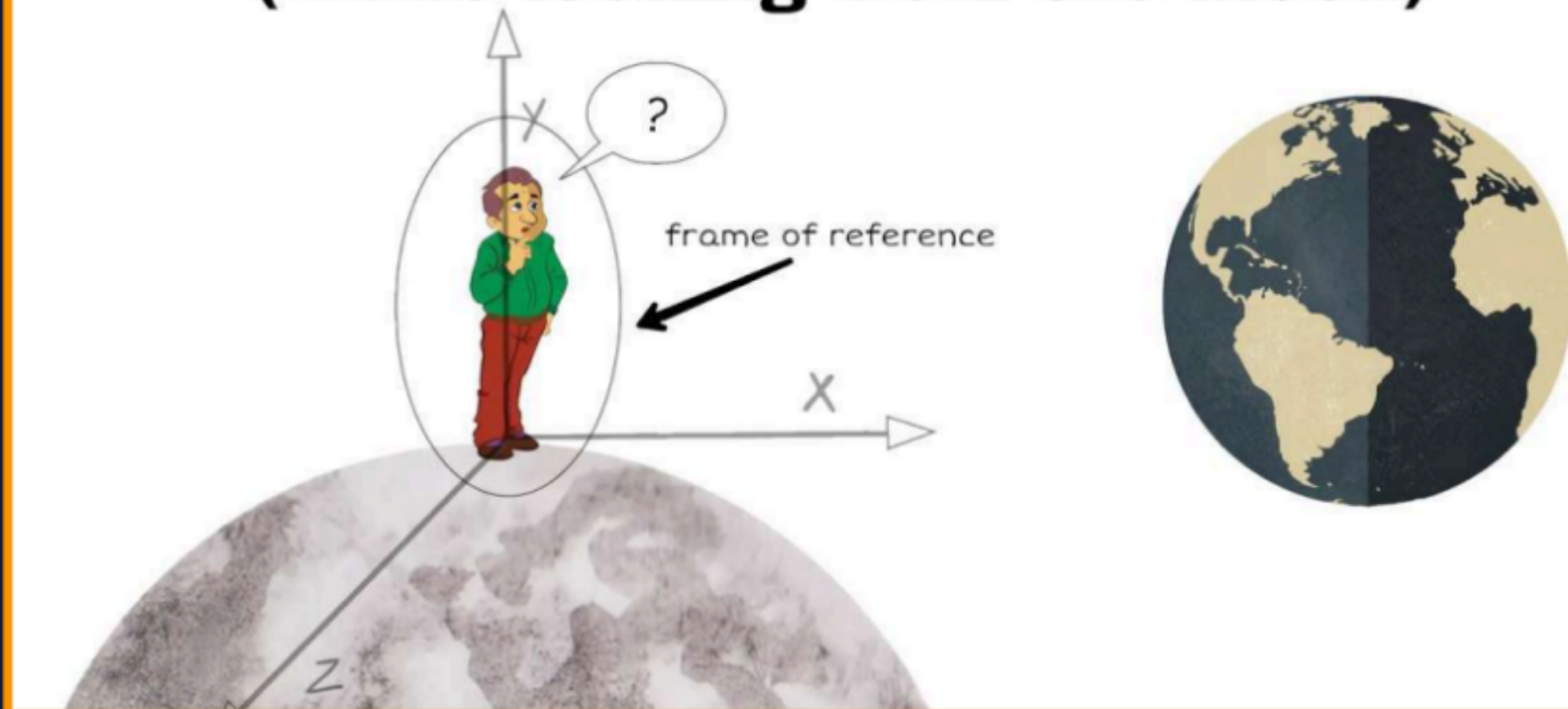


An aeroplane is the frame of reference
(As the observer is looking from an aeroplane)

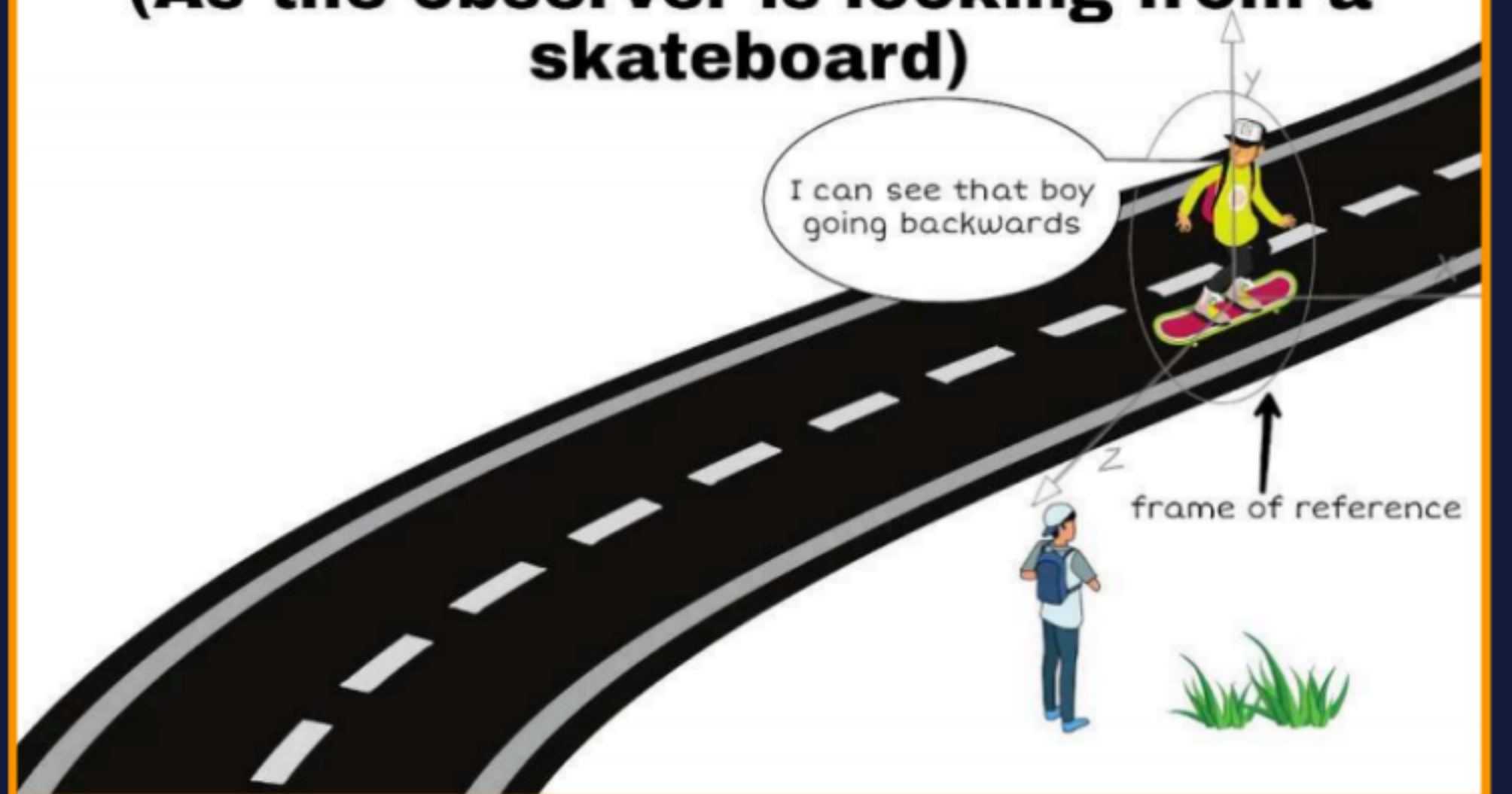




Why does the **earth appear to be moving?
(While looking from the moon)**



**A skateboard is the frame of reference
(As the observer is looking from a skateboard)**



Types of Frames of Reference:

→ Inertia
Inertial frame of reference: → Rest + Same Motion

An inertial frame of reference is a concept in physics that refers to a frame in which Newton's first law of motion holds true.



**A bike is in inertial frame of reference
(As a bike is at rest)**



Non-inertial reference frame:

A non-inertial reference frame is a concept in physics that refers to a frame of reference that is subjected to acceleration.



**A bike is in non inertial frame of reference
(As a bike is accelerated)**

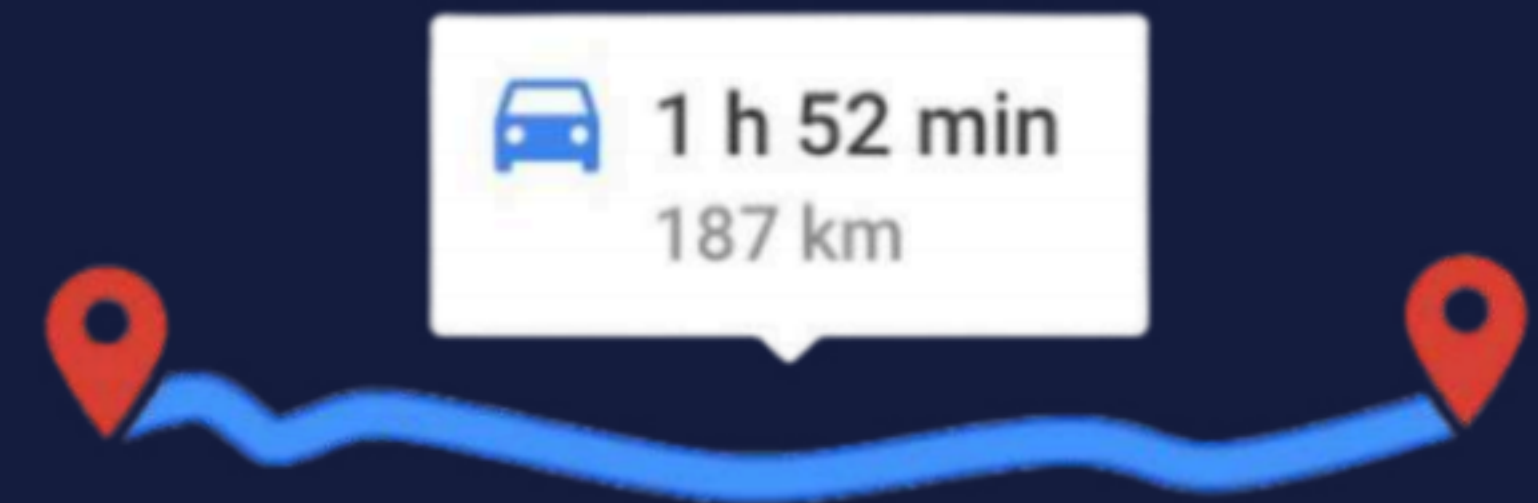


Distance

Distance is the total length of the actual path traveled by an object, irrespective of direction.

SI Unit = meter (m).

Example = Walking 3m east and then 4 m north \rightarrow Distance = $3 + 4 = 7\text{m}$.



Displacement

Displacement is the shortest straight-line distance from the initial to the final position of the object, considering direction.

SI Unit = meter (m).

$$\sqrt{9+16} = \sqrt{25} = 5$$

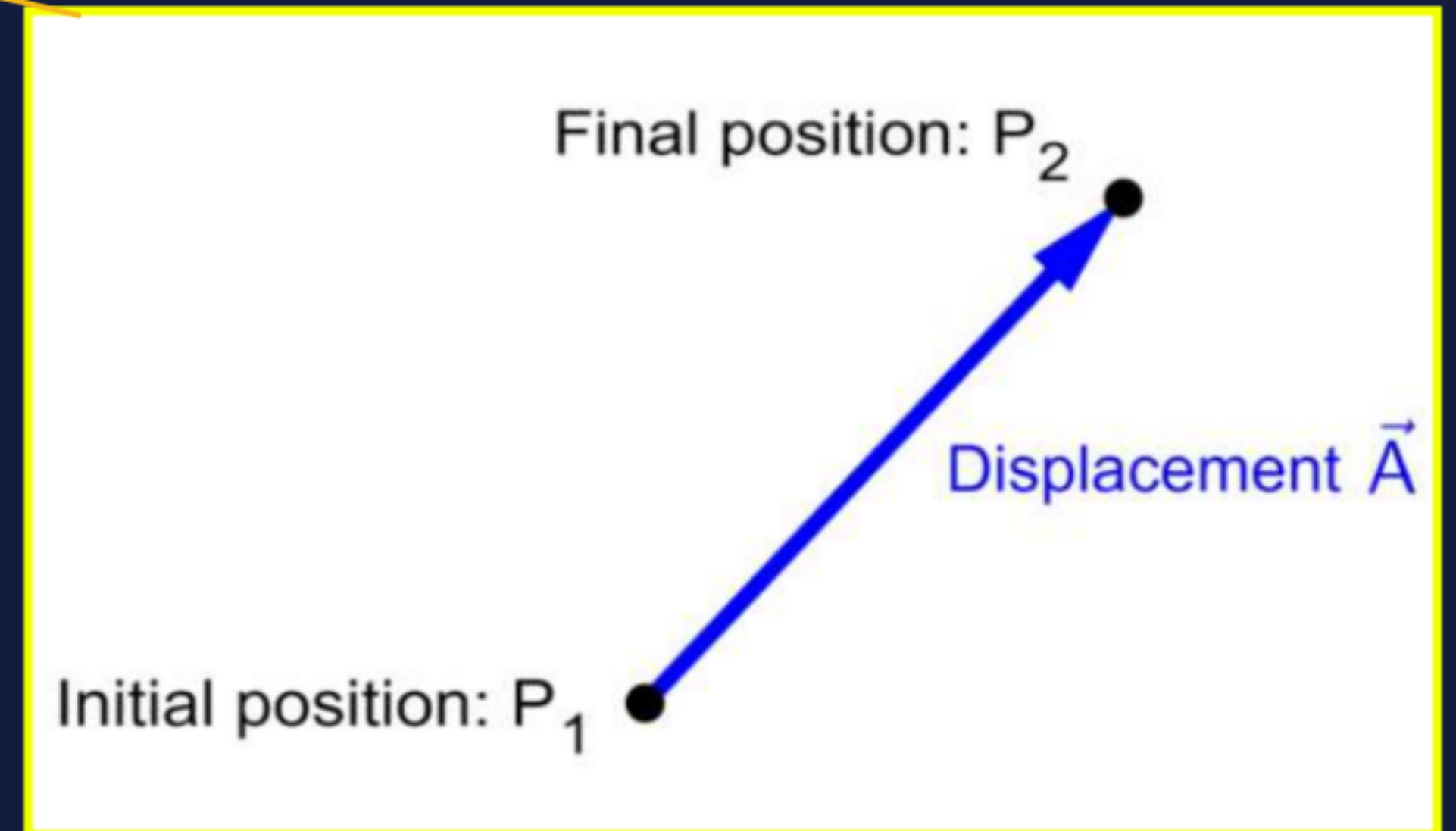


3 Km

4 Km

5 Km

Formula = $\Delta s = s_2 - s_1$ (change in position).



DISTANCE AND DISPLACEMENT IN CIRCULAR PATH:

$$l_1 = 44 \text{ m}$$

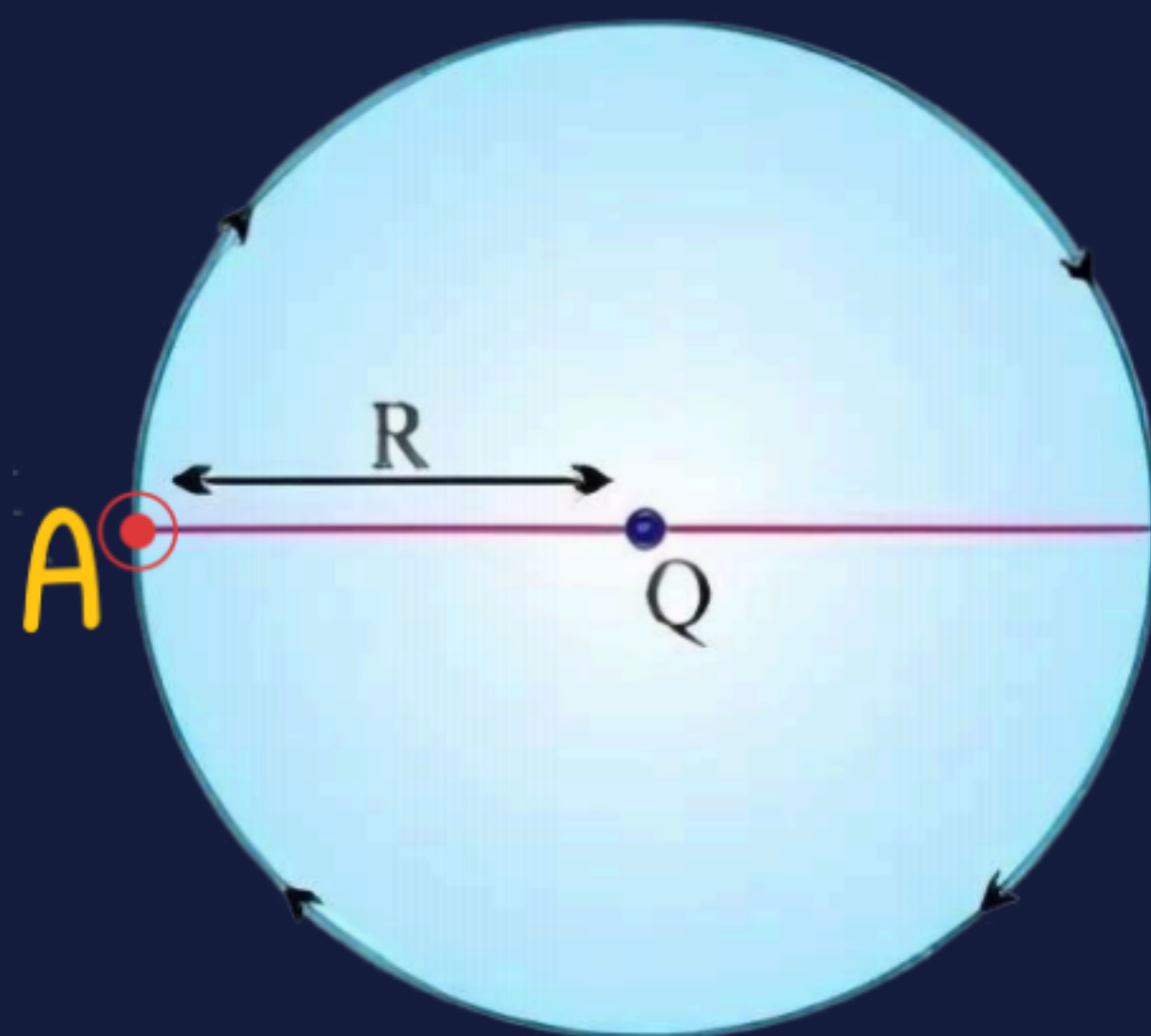
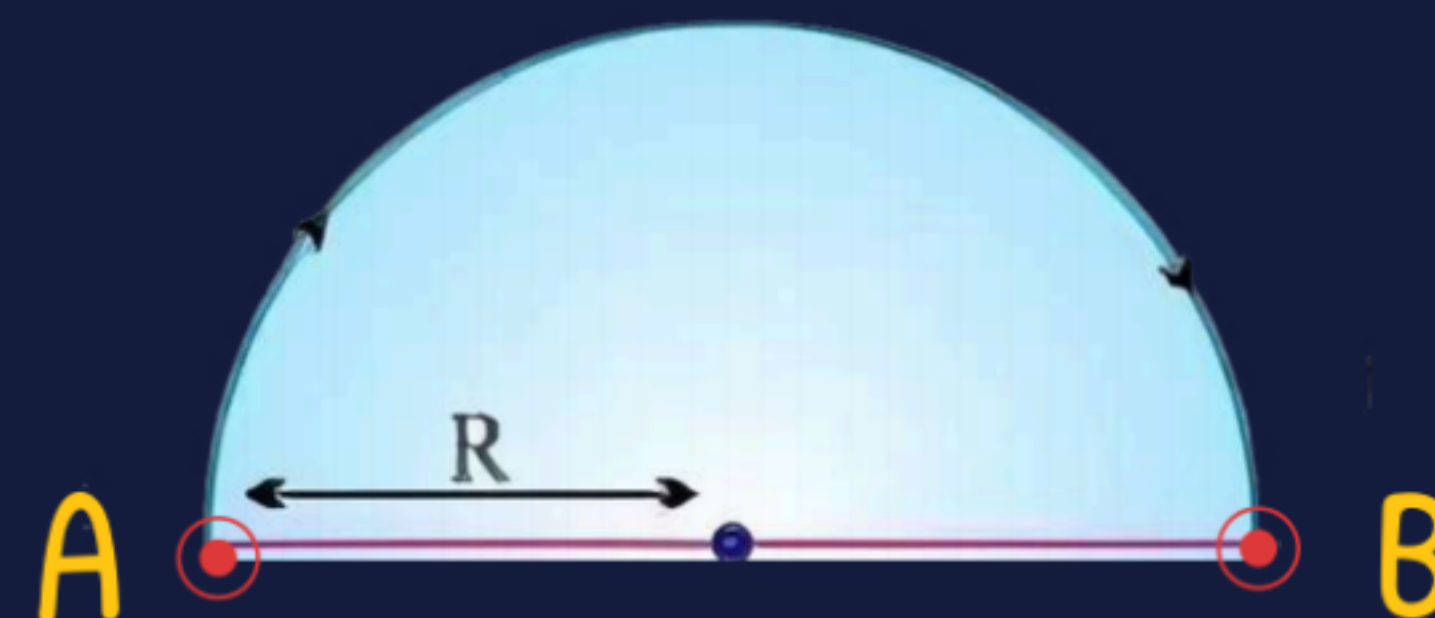
$$= 2\pi r$$

Semi Circle (A to B)

- Distance (D) = Circumference/2 = πr
- Displacement (s) = $2r$

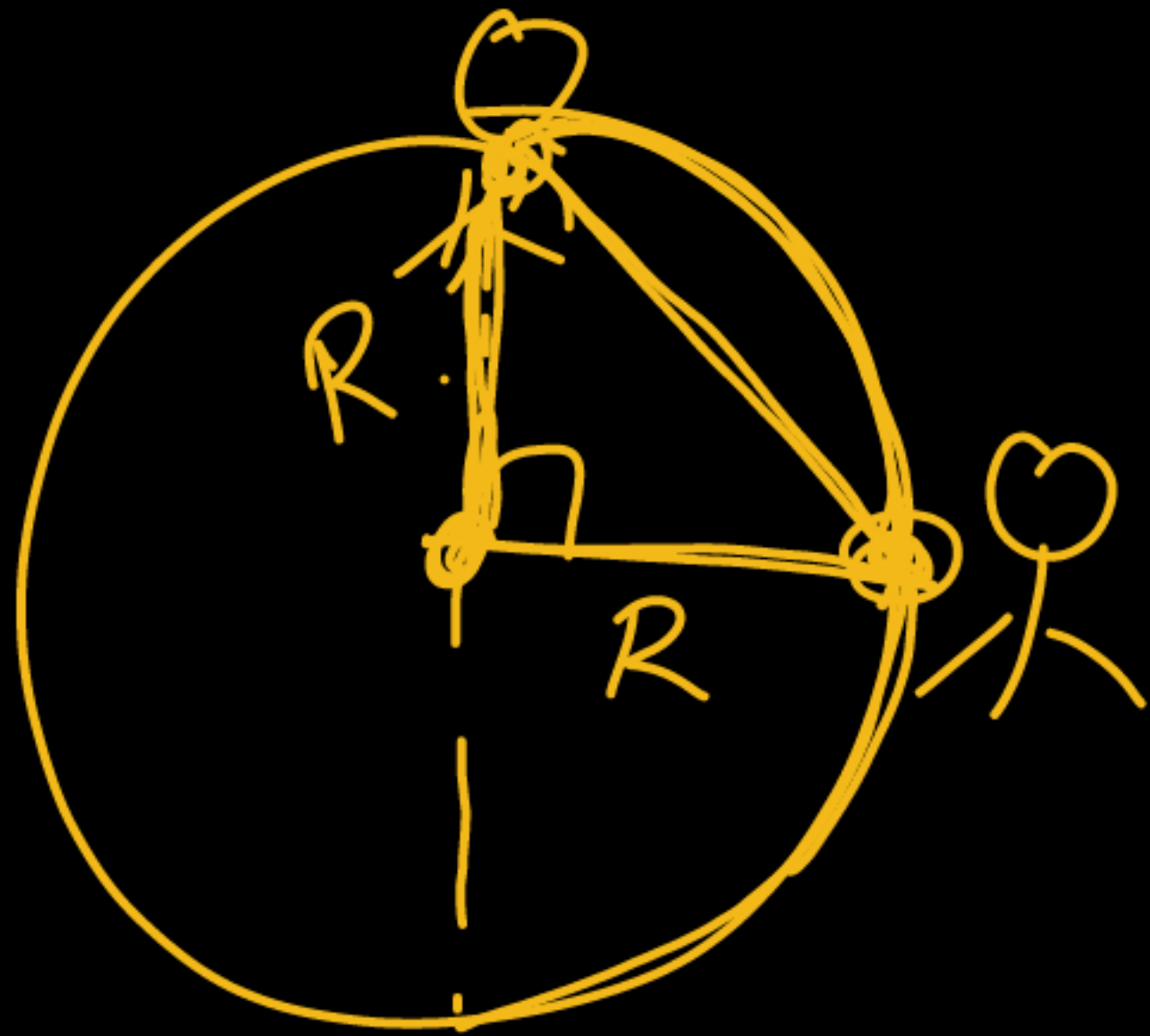
$$= 2\pi r$$

$$= 2 \times \frac{22}{7} \times 7 = 44 \text{ m}$$



Full Circle(A to A)

- Distance (D) = Circumference = $2\pi r$
- Displacement (s) = 0 (starts and ends at the same point).



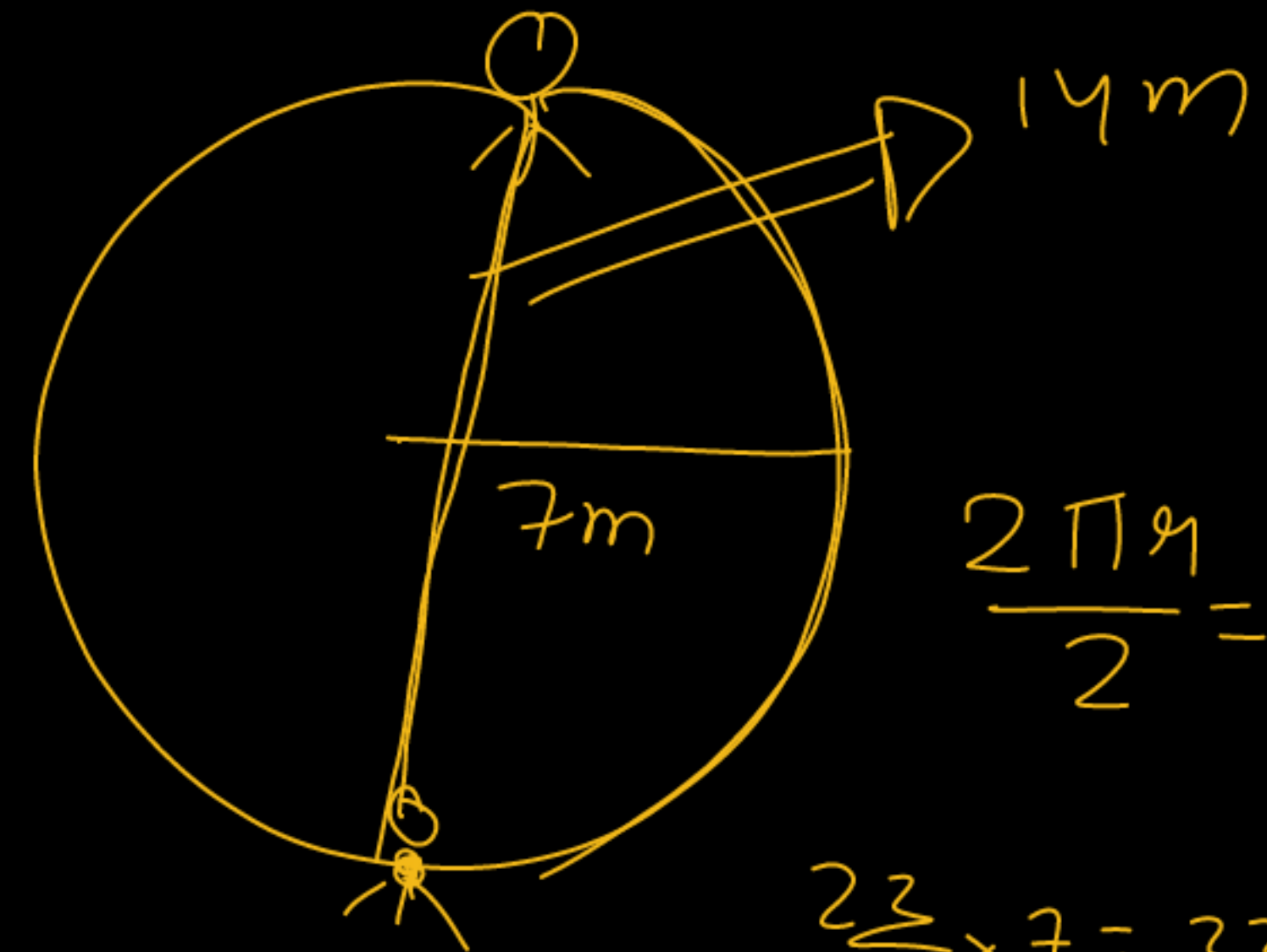
$$\sqrt{49+49}$$

$$= \sqrt{98}$$

$$\pi \times r = \pi \frac{r}{2} \times 2$$

$$= \frac{22}{7} \times 2 \times 7$$

$$= \underline{11m}$$



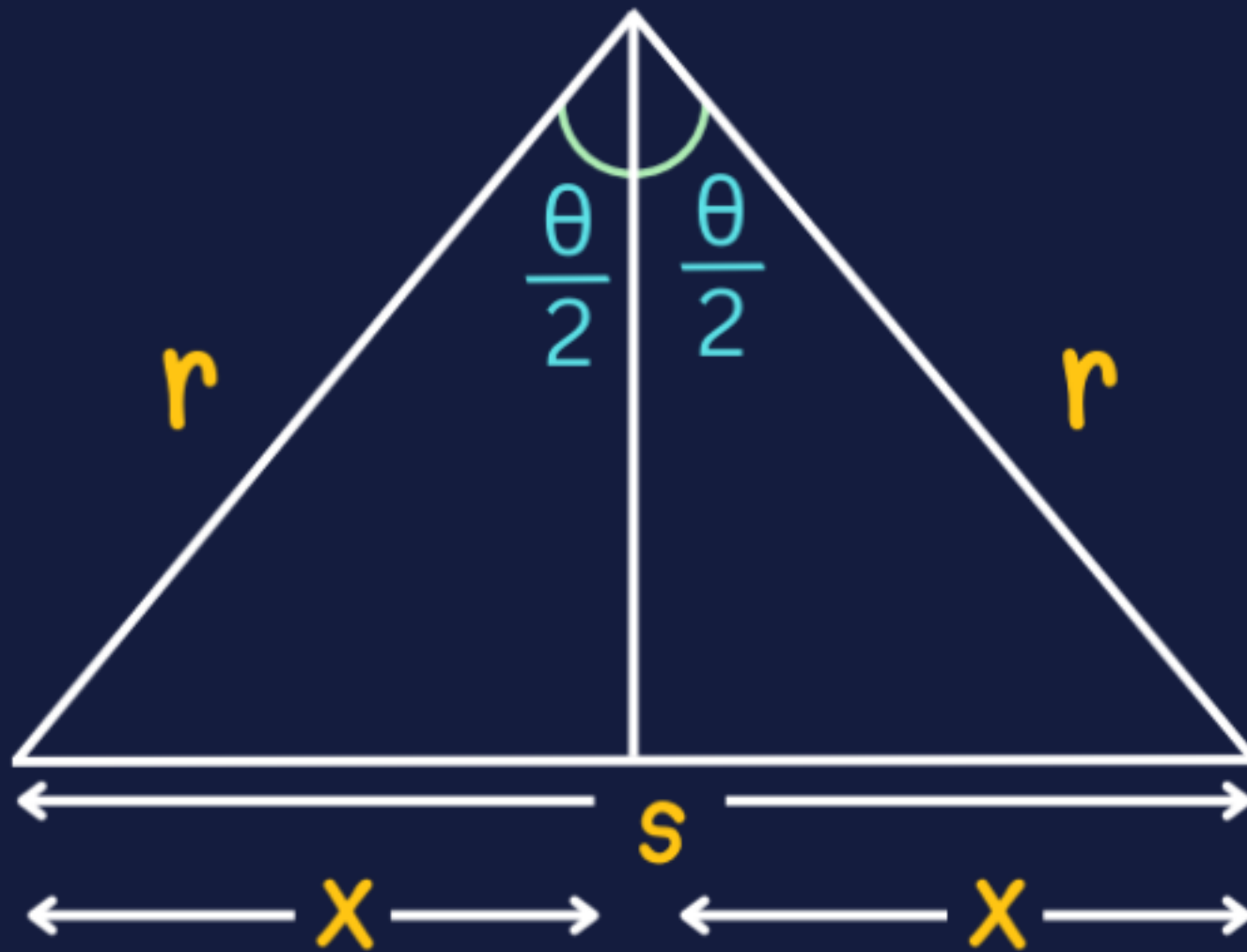
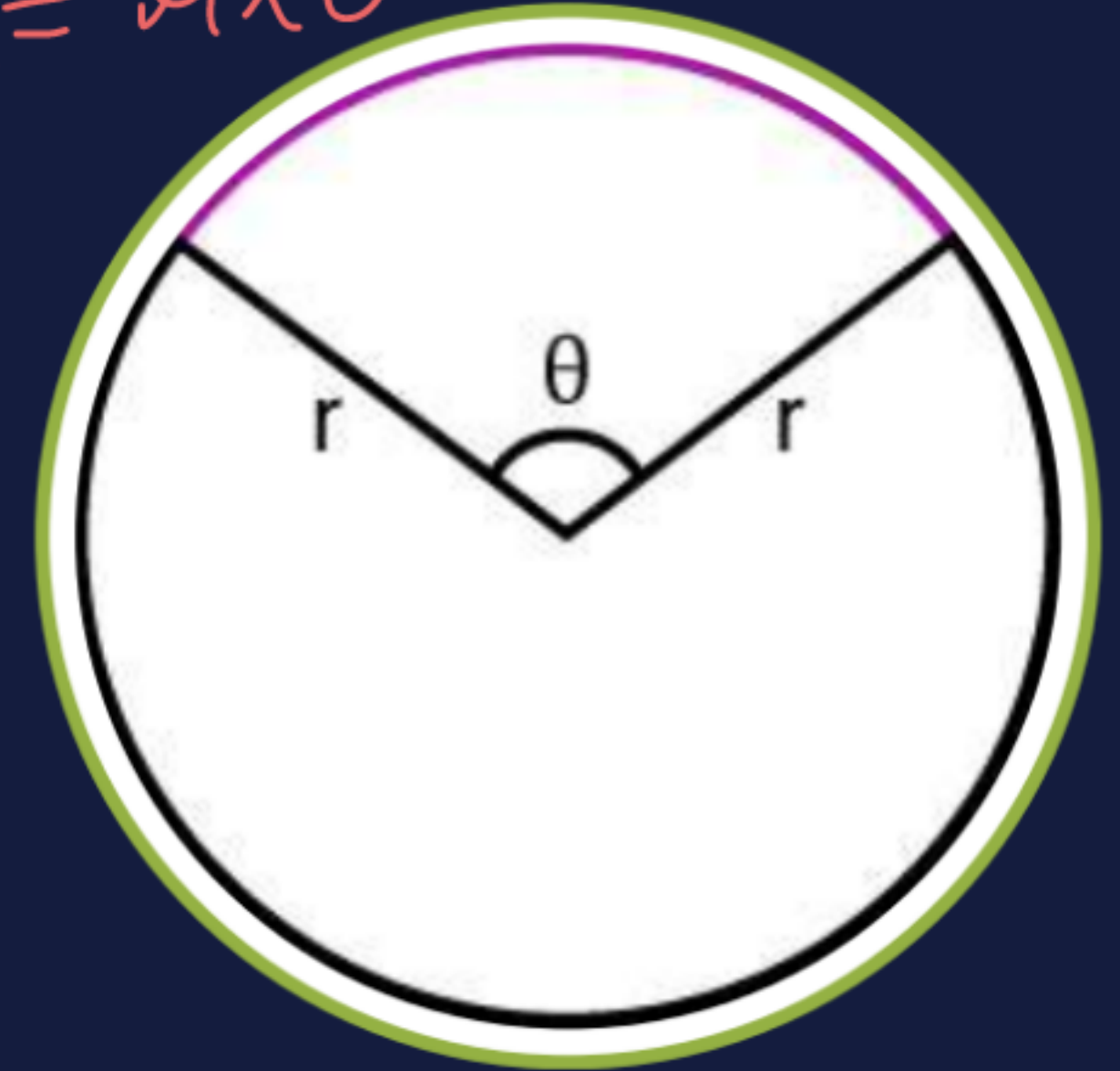
$$\frac{2\pi r}{2} = \pi r$$

$$\frac{22}{7} \times 7 = \underline{22m}$$

DISTANCE AND DISPLACEMENT IN CIRCULAR ARC:

$$l = r \times \theta$$

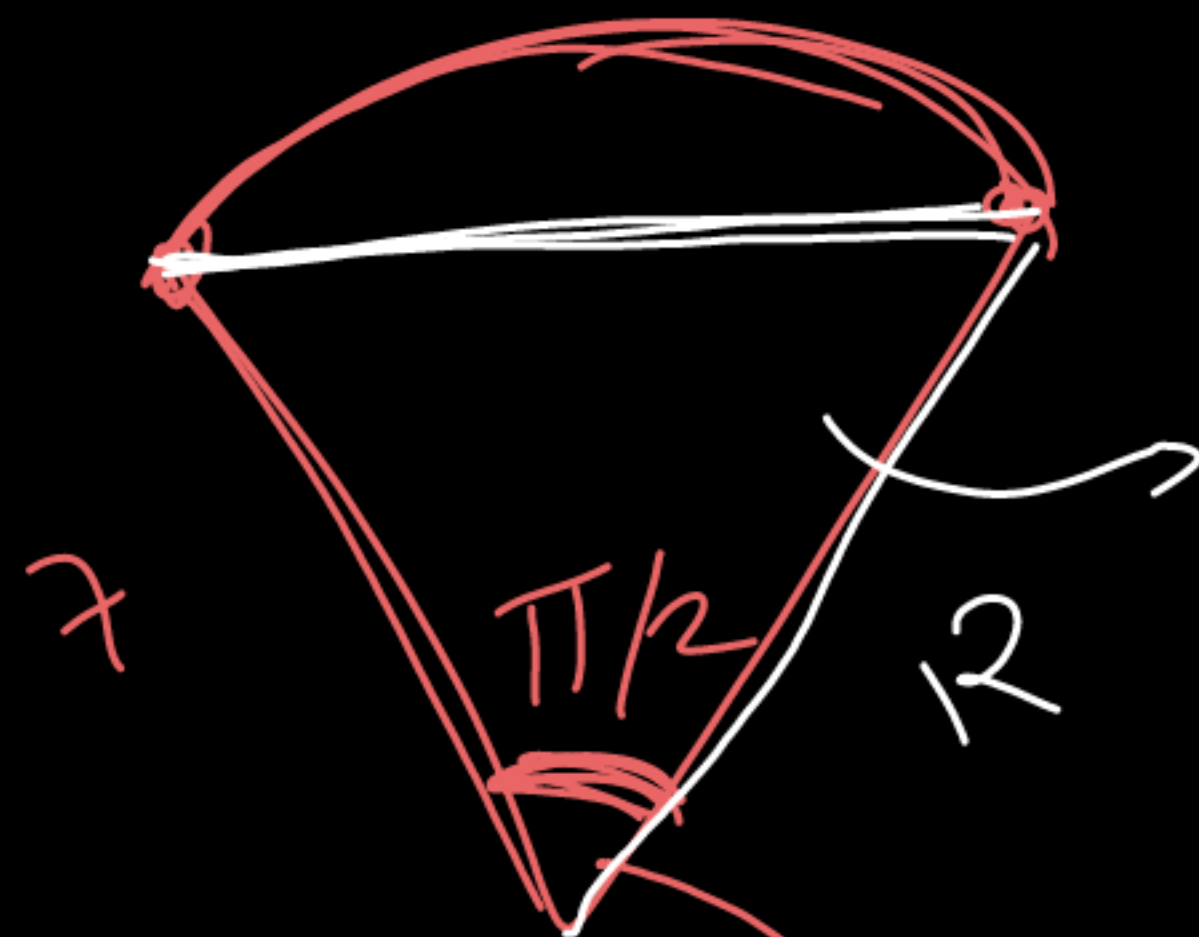
- Arc Length (Distance): $D = R\theta$ (θ in radians)
- Displacement (chord length): $\Delta = 2R\sin\left(\frac{\theta}{2}\right)$



Since, $\sin\theta = \frac{P}{H}$

$$\sin\left(\frac{\theta}{2}\right) = \frac{x}{R} \Rightarrow x = R \sin\left(\frac{\theta}{2}\right) \Rightarrow \Delta = 2x = 2R \sin\left(\frac{\theta}{2}\right)$$

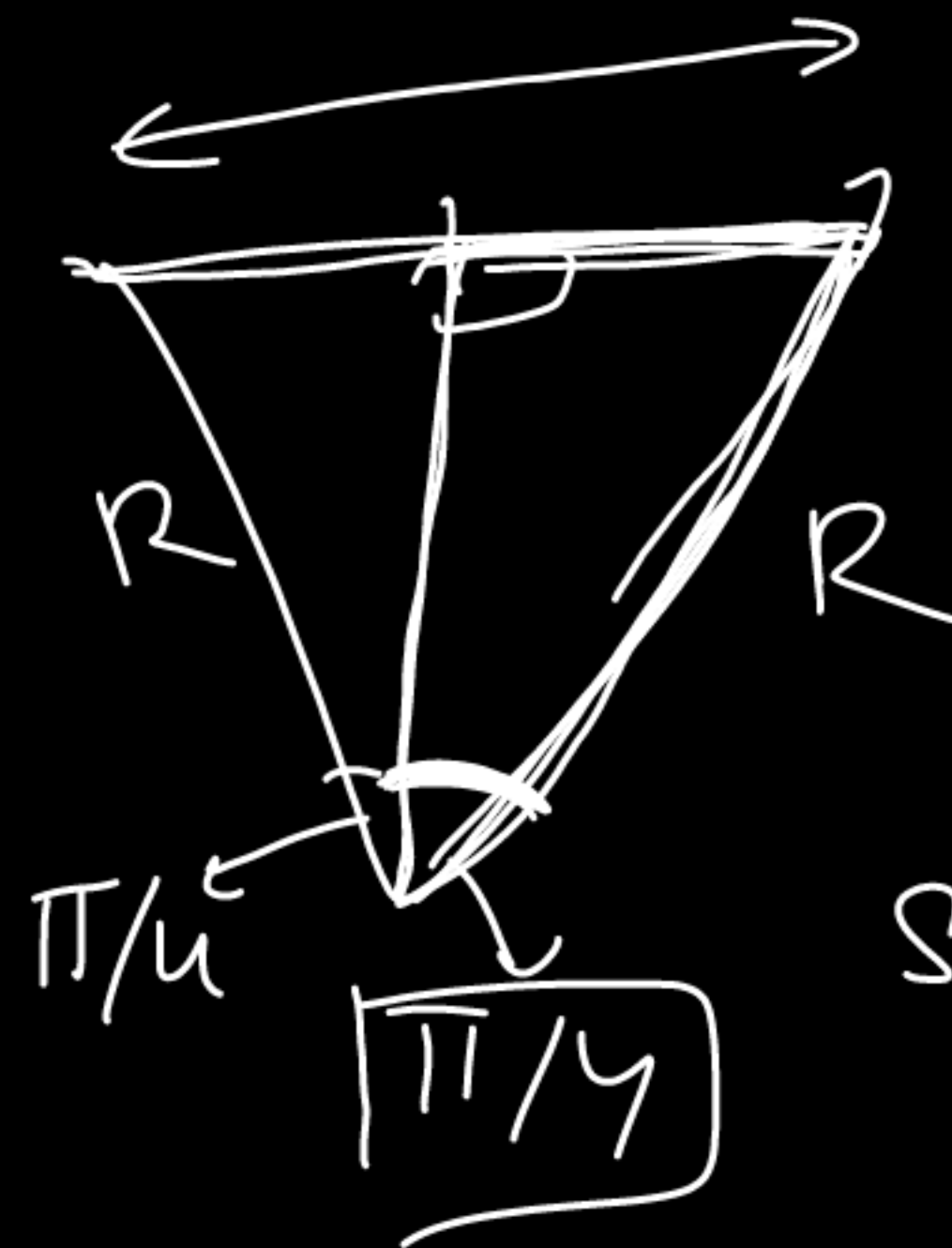
②



$$l = 7 \times \frac{\pi}{2}$$

$$l = 7 \times 22$$

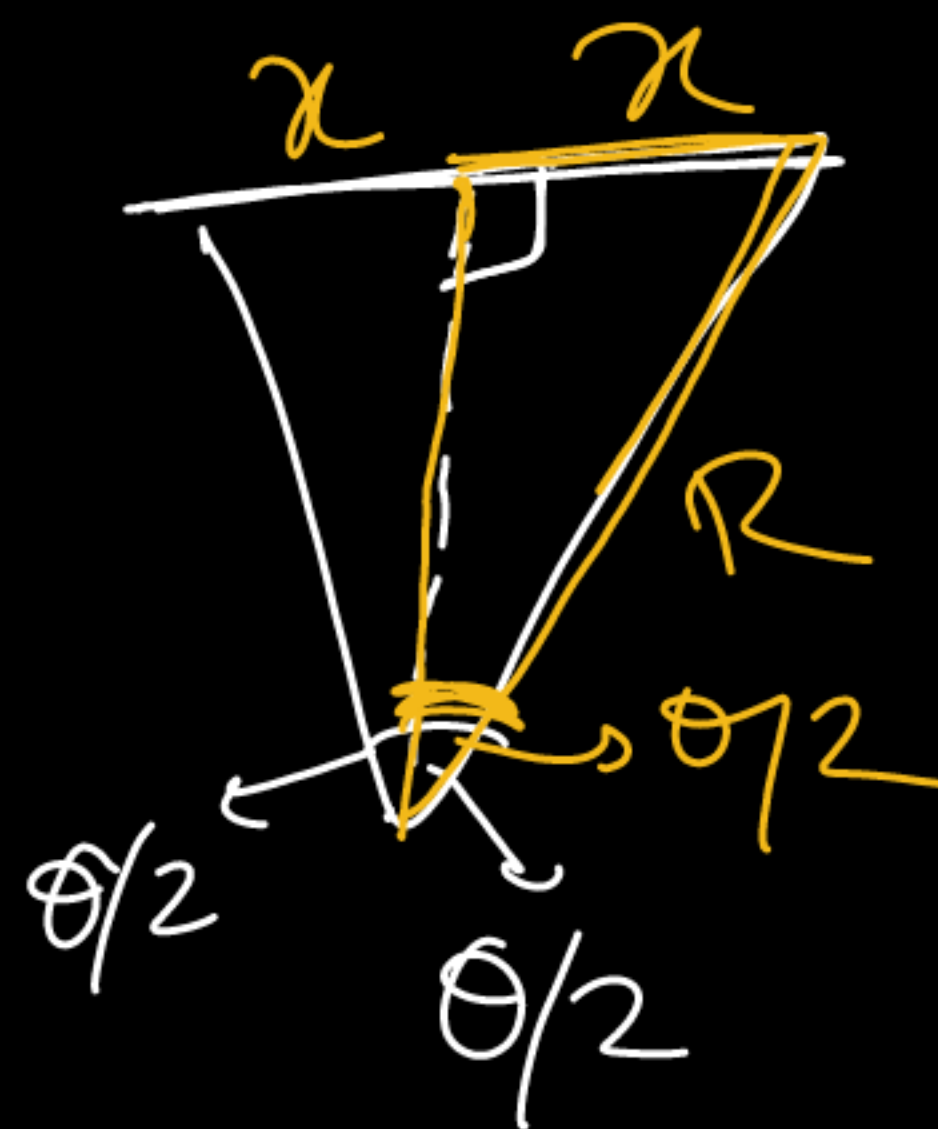
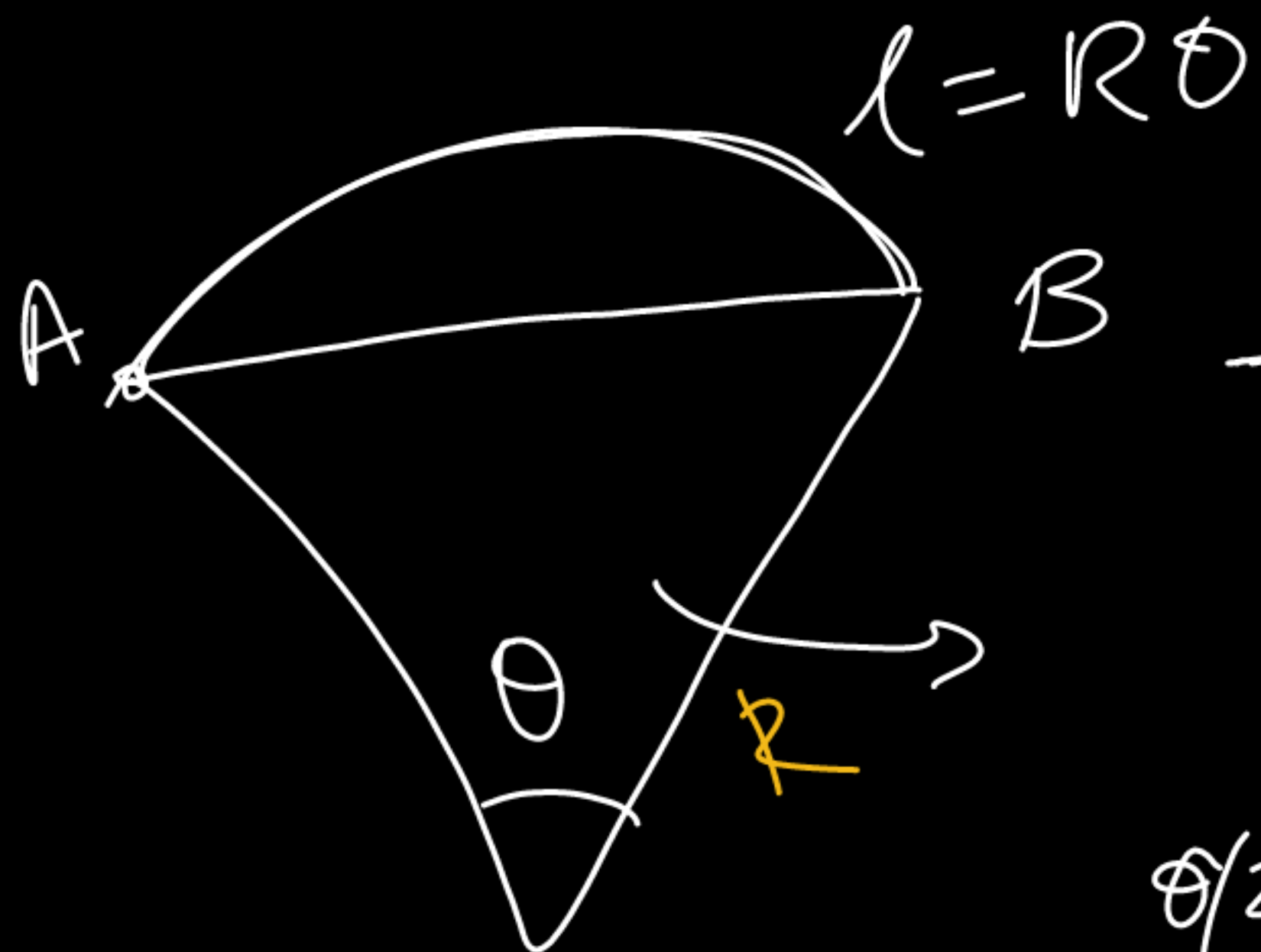
$$l = 154$$



$$\sin \frac{\pi}{4} = \frac{P}{R}$$

$$P = R \sin \frac{\pi}{4}$$

$$2 R \sin \frac{\pi}{4}$$

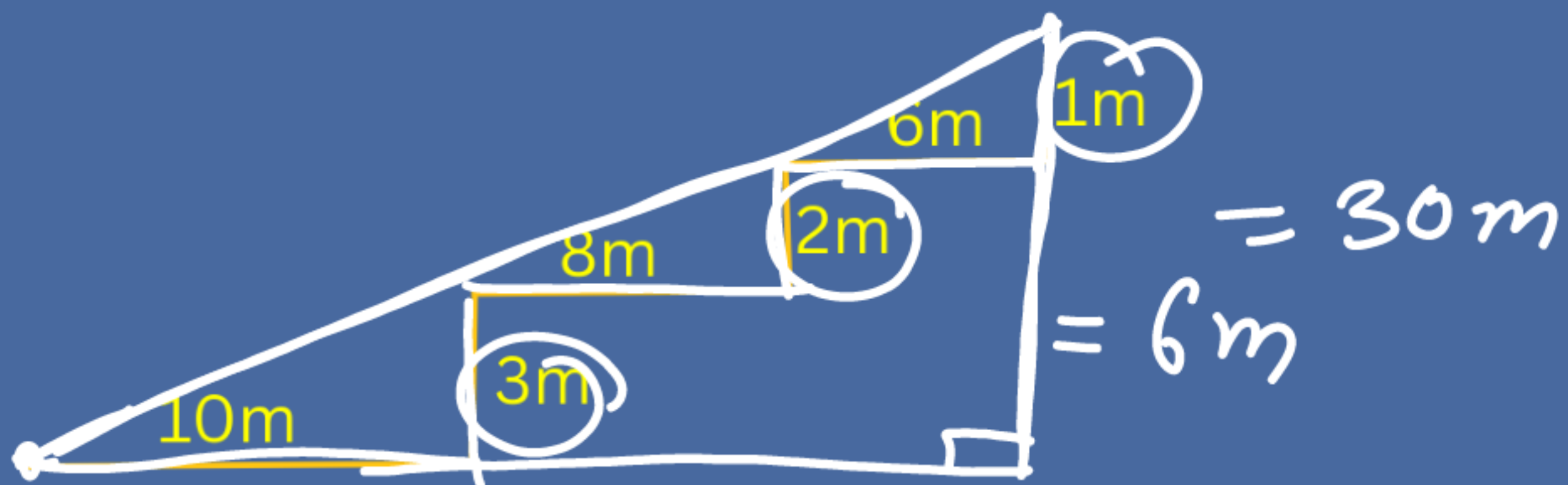


$$\sin\left(\frac{\theta}{2}\right) = \frac{x}{R}$$

$$x = R \sin\left(\frac{\theta}{2}\right)$$

$$= 2R \sin\left(\frac{\theta}{2}\right)$$

Ques. find distance and displacement ?



 SOLUTION

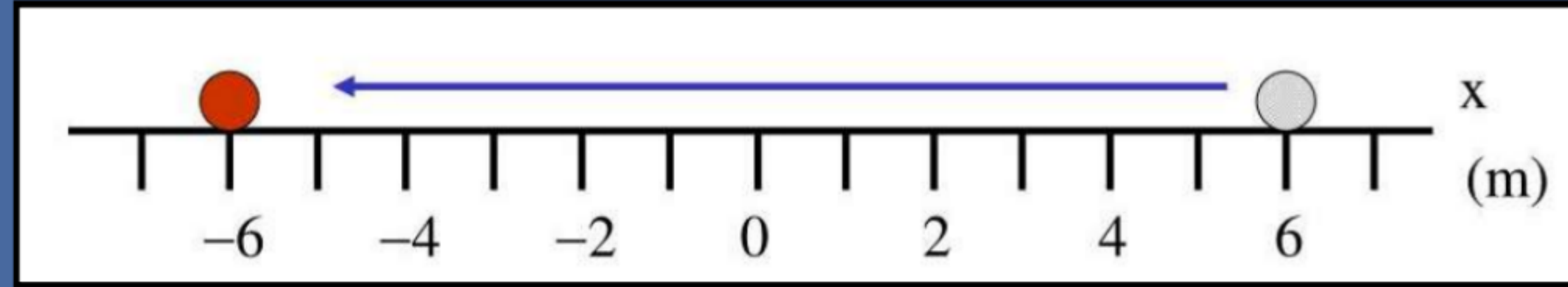
↓
24m

$$\sqrt{36 + (24)^2} \quad 576$$

$$\sqrt{612}$$



Ques. Calculate displacement.



 SOLUTION



Ques. A person walks 5 km north, then 3 km south, and finally 2 km north.

(i) What is the total distance travelled?

(ii) What is the displacement of the person from the starting point?



 SOLUTION

$= 4 \text{ km}$



10 Km



Ques. A person walks along a circular path of radius 10 m for an angle of 90° . Calculate distance and displacement.

 SOLUTION

$$\theta = 90^\circ \Rightarrow \pi/2$$

$$r = 10\text{m}$$



$$l = 10 \times \frac{\pi}{2}$$

$$s = 2R \sin\left(\frac{\theta}{2}\right)$$

$$= 2 \times 10 \sin(45^\circ)$$

$$= \frac{20}{\sqrt{2}}$$

$$= \underline{10\sqrt{2}}$$



Speed

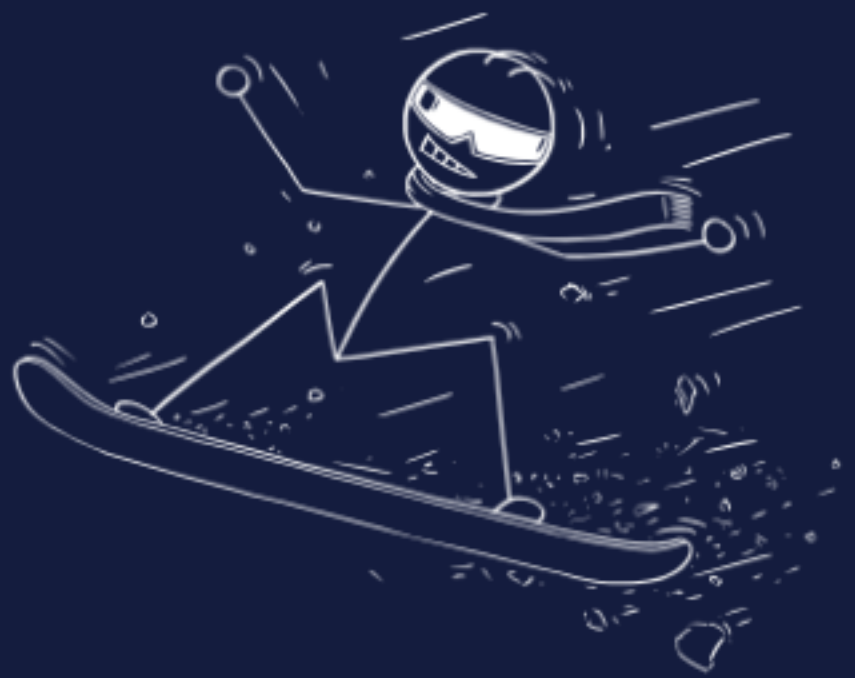
→ Scalar

Speed is the rate of change of distance with respect to time.

It tells us how much distance an object covers in a given time interval.

SI Unit = m/s

Formula = $\text{Speed} = \frac{\text{Distance traveled}}{\text{Time taken}}$



Distance When its Divided by Time:



Velocity

⇒ Vector

Velocity is the rate of change of displacement with respect to time.

Unlike speed, velocity considers direction, making it a **vector quantity**.

SI Unit = m/s

Formula = $\text{Velocity} = \frac{\text{Displacement}}{\text{Time taken}}$


⊗ ⇒ Straight line
Motion

⊗ = ⊙

Distance = displacement



AVERAGE SPEED:



A diagram showing a car moving from point A to point B and back to A. The distance from A to B is 200 km, and the time taken is 1 hr. The distance from B to A is 100 km, and the time taken is 2 hr. The calculation for average speed is shown as $\frac{300}{3} = 100$.

$$\frac{200 \text{ km} + 100 \text{ km}}{1 \text{ hr} + 2 \text{ hr}} = \frac{300}{3} = 100$$

The total distance traveled by an object divided by the total time taken. It gives the rate at which an object covers distance.

Nature: Scalar quantity (only magnitude, no direction).

SI Unit: meters per second (m/s).

Dimensional Formulae: LT^{-1}

Conversion of units from Km/hr to m/s :

$$Km/hr \xrightarrow{5/18} m/s$$

The conversion factor $5/18$ is shown above the arrow, and the inverse factor $18/5$ is shown below the arrow.

$$\text{Avg. Speed} = \frac{\text{Total Distance}}{\text{Total Time Taken}}$$



AVERAGE VELOCITY:

The total displacement of an object divided by the total time taken. It gives the rate at which an object changes its position.

Nature: Vector quantity (has both magnitude and direction).

SI Unit: meters per second (m/s).

Dimensional Formulae: LT^{-1}

$$V_{avg} = \frac{u + v}{2}$$

$$\text{Avg. Velocity} = \frac{\text{Total Displacement}}{\text{Total Time Taken}}$$

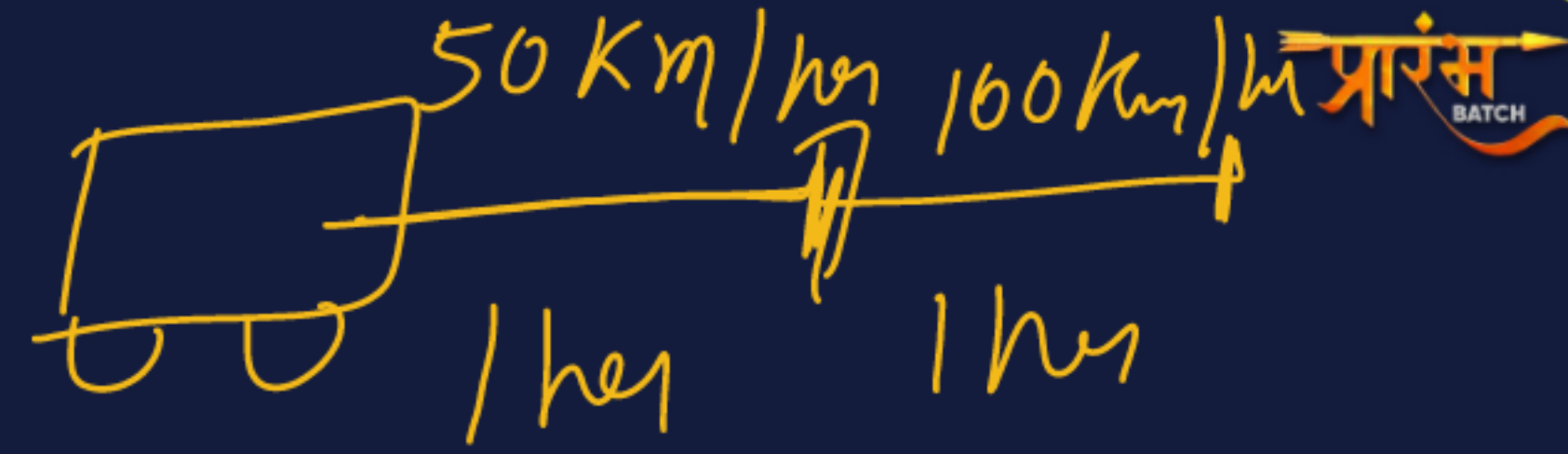
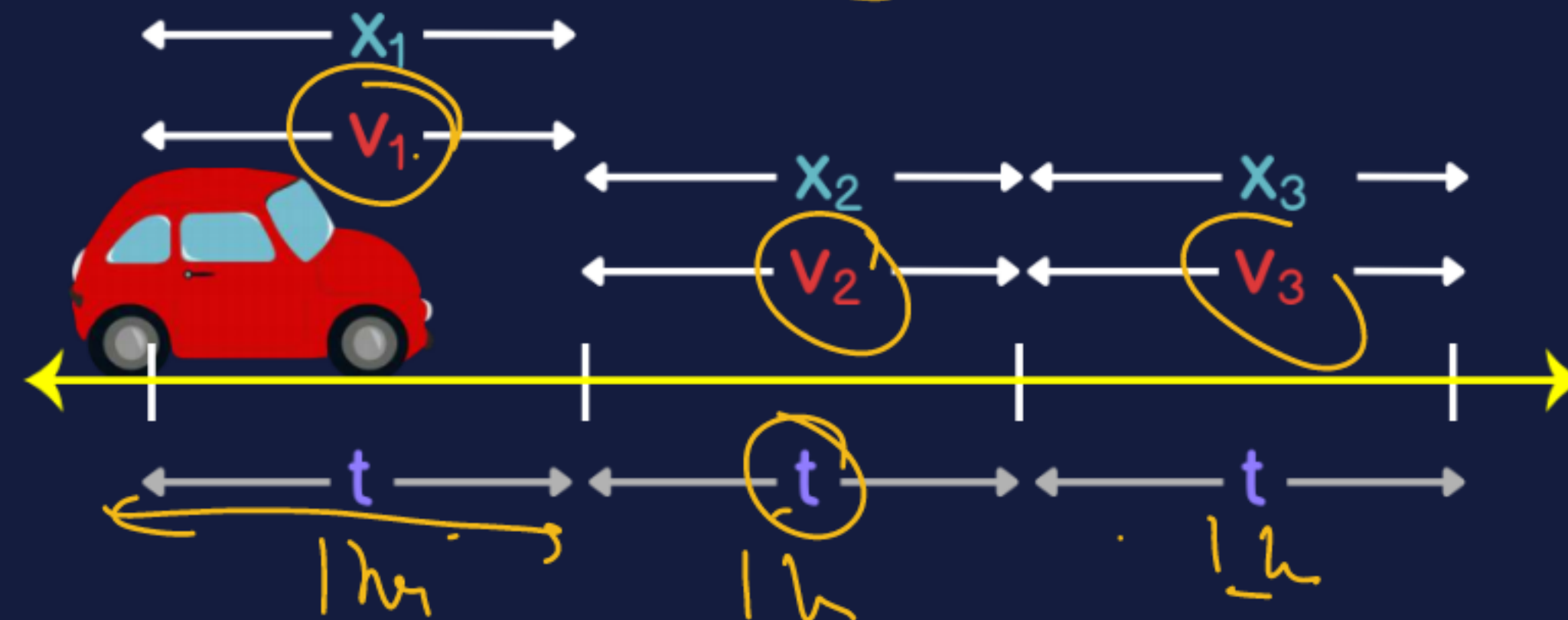


SPECIAL CASES:

1. Case When Time Intervals Are Equal

If a journey is divided into equal time intervals t , but different speeds are maintained in each segment:

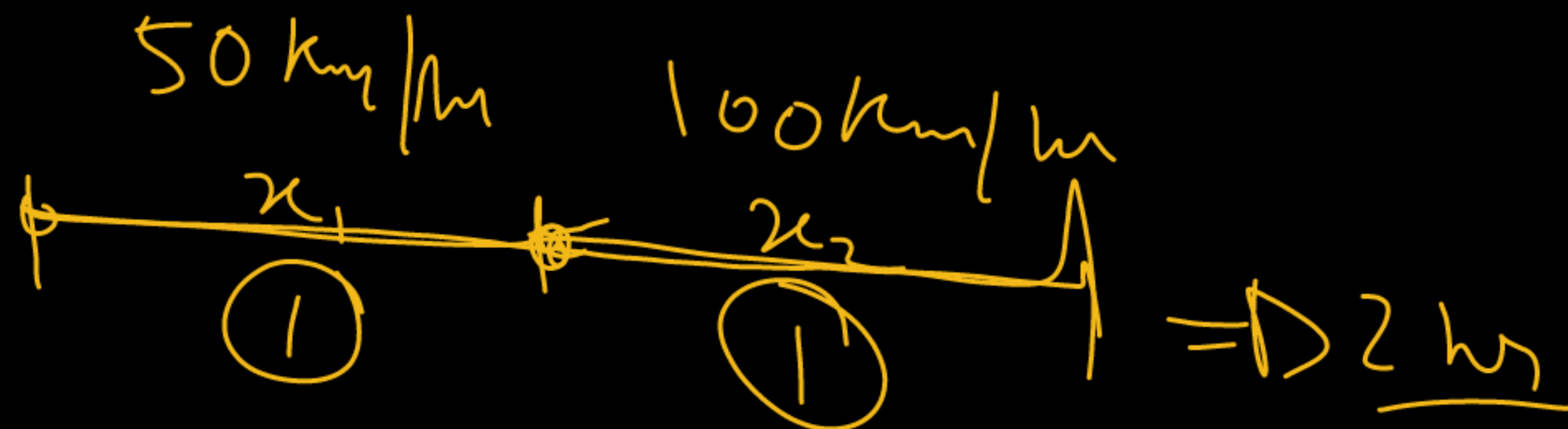
$$V_{\text{avg}} = \frac{V_1 + V_2 + V_3 + \dots + V_n}{n}$$



$$\frac{\text{total } d}{\text{total } t} = \frac{150}{2} = \underline{75 \text{ km/h}}$$

$$x_1 = 50 \times 1$$

$$x_1 = 50 \text{ km}$$



$$x_2 = 100 \times 1$$

$$= 100 \text{ km}$$

Distance in each segment: $x_i = V_i \cdot t$

Total distance:

$$D = x_1 + x_2 + \dots + x_n = t(V_1 + V_2 + \dots + V_n)$$

Total time:

$$T = nt$$

So,

$$V_{\text{avg}} = \frac{D}{T} = \frac{t(V_1 + V_2 + \dots + V_n)}{nt} = \frac{V_1 + V_2 + \dots + V_n}{n}$$

2. Case When Distance Segments Are Equal

If a journey is divided into equal distance intervals, but at different speeds:

- Let each segment have a distance x
- Speeds: $V_1, V_2, V_3, \dots, V_n$
- Time taken in each segment: $t_1 = \frac{x}{V_1}, t_2 = \frac{x}{V_2}, \dots$

$$t = \frac{x}{V_1}$$

$$\frac{2 \times 100}{\dots}$$



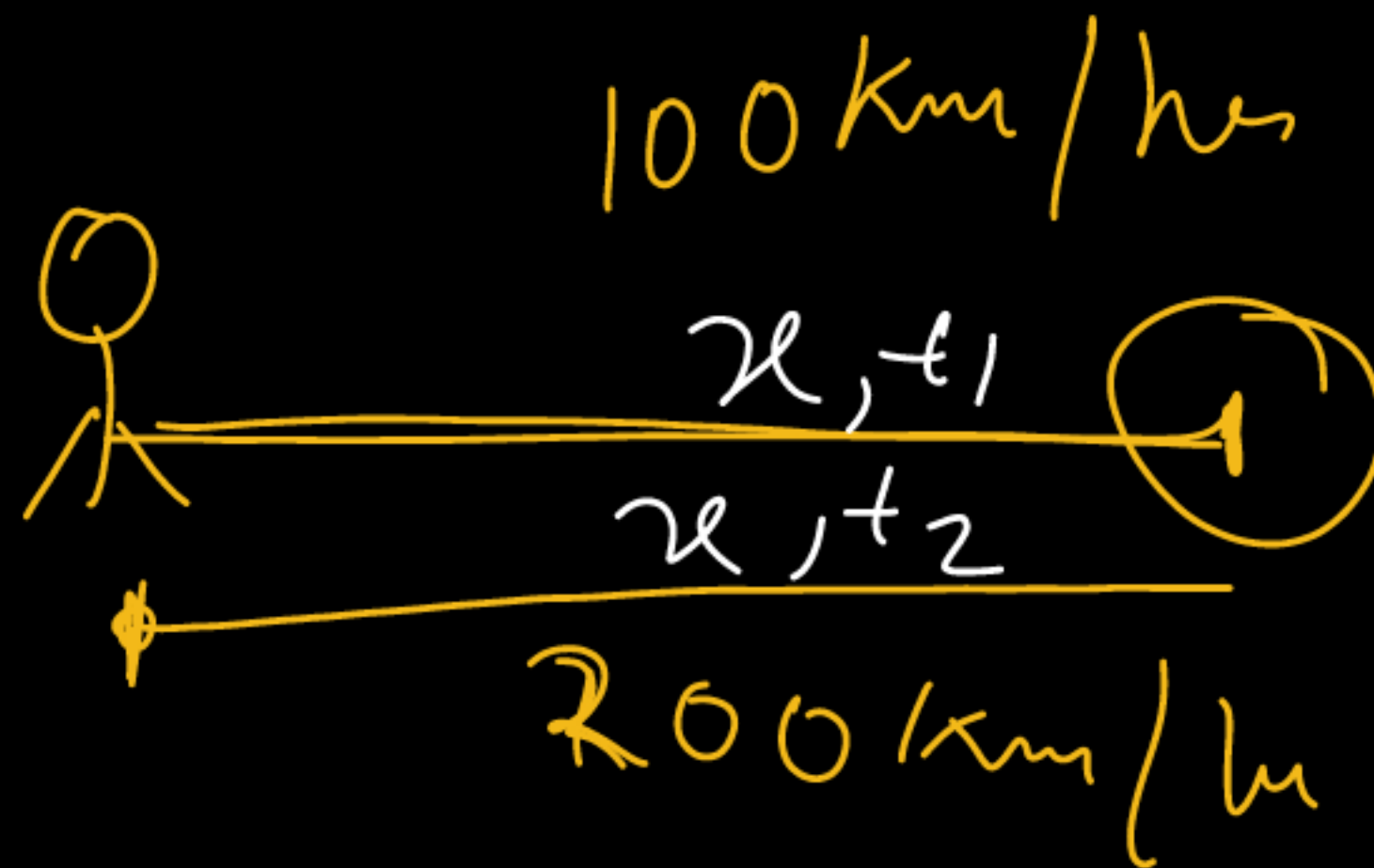
$$\frac{2}{\frac{1}{100} + \frac{1}{200}}$$

So,

$$V_{\text{avg}} = \frac{\text{Total Distance}}{\text{Total Time}} = \frac{n \cdot x}{\frac{x}{V_1} + \frac{x}{V_2} + \dots + \frac{x}{V_n}} = \frac{n}{\left(\frac{1}{V_1} + \frac{1}{V_2} + \dots + \frac{1}{V_n} \right)}$$

3rd case

$$avg = \frac{\text{total } q}{\text{total } t} = \frac{2x}{3x}$$



$$= \frac{\frac{2x}{3x}}{200}$$

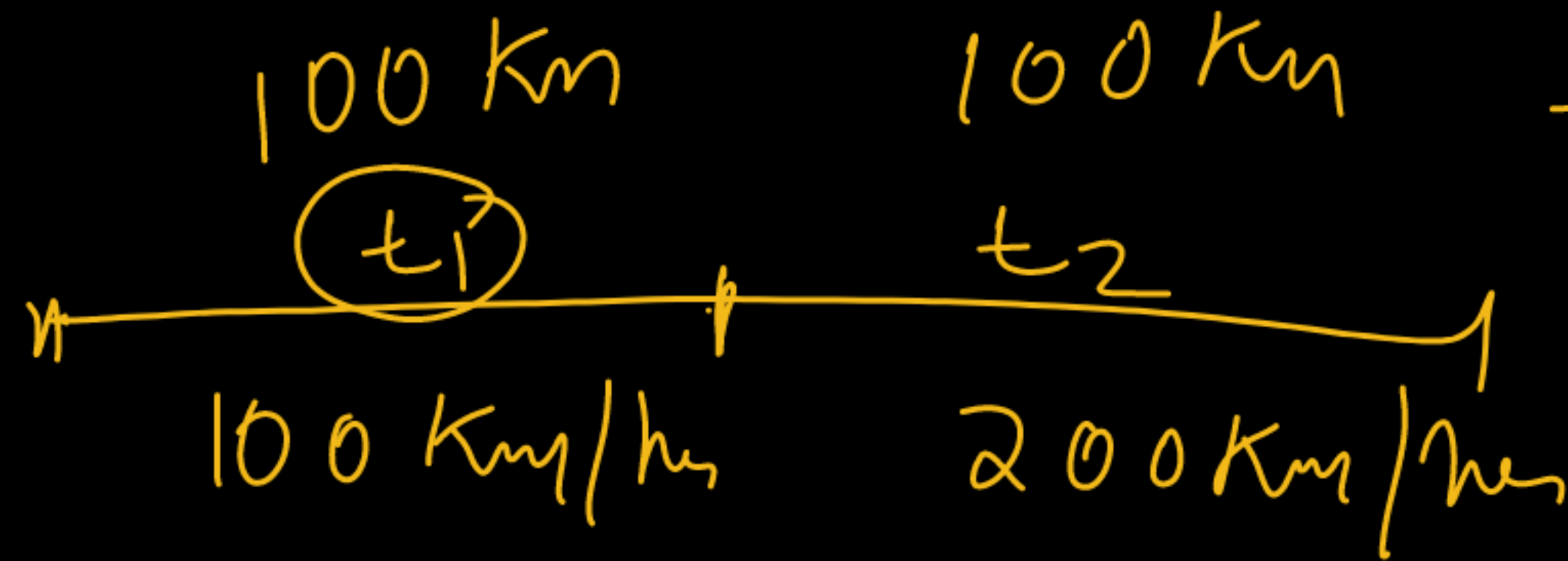
$$= \frac{400}{3} = 133.33$$

$$t_1 = \frac{x}{100}$$

$$t_2 = \frac{x}{200}$$

$$\frac{x}{100} + \frac{x}{200} = \frac{3x}{200}$$

$$t_1 = \frac{100}{100} = 1 \text{ hr}$$



$$t_2 = \frac{100}{200} = \frac{1}{2} = \underline{\underline{0.5}}$$

$$Avg = \frac{\text{total } d}{\text{total } t} = \frac{200}{1.5} = \underline{\underline{133.33}}$$

Ques. A car moves from point A to point B which is 100 m apart in a straight line. It then returns back from B to a point C which is 40 m away from A (on the same path).

The entire journey takes 20 seconds.

- (i) What is the total distance travelled by the car?
- (ii) What is the magnitude of displacement?
- (iii) What is the average speed and average velocity?



Ques. A car travels 30km at a uniform speed of 40km/h and the next 30km at a uniform speed of 20km/h . Find its average speed

- A. 26.7 Km/h
- B. 2.67 Km/h
- C. 48.7 Km/h
- D. 267 Km/h



 SOLUTION

$$\frac{n}{\frac{1}{v_1} + \frac{1}{v_2} + \dots} = \frac{2}{1}$$



Ques. A car moves a distance of 200 km . it covers the first -half of the distance at speed 40 km/h and the second -half of distance at speed $v\text{ km/h}$. the average speed is 48 km/h . Find the value of v [CBSE AIPMT 1991]

- A. 56 km/h
- B. 60 km/h
- C. 50 km/h
- D. 48 km/h



 SOLUTION

Diagram showing a distance of 200 km split into two halves of 100 km each. The first half is traveled at 40 km/h and the second half at $v\text{ km/h}$. The average speed is 48 km/h .

$$\frac{n}{\frac{1}{v_1} + \frac{1}{v_2}} = \frac{2}{\frac{1}{40} + \frac{1}{v}} = 48$$



Ques. A car moves from X to Y with a uniform speed v_1 , and returns to X with a uniform speed v_2 . The average speed for this round trip is: [CBSE AIPMT 2007]

A) $2v_d v_u / (v_d + v_u)$

B) $(v_u v_d) / 2$

C) $\sqrt{(v_u v_d)}$

D) $(v_d + v_u) / 2$



→ Reference Point

Ques. A police van moving on a highway with a speed of 30 km h^{-1} fires a bullet at a thief's car speeding away in the same direction with a speed of 192 km h^{-1} . If the muzzle speed of the bullet is 180 km h^{-1} , with what speed does the bullet hit the thief's car? (Note: Obtain that speed which is relevant for damaging the thief's car). [NCERT]

 SOLUTION

$$210 - 192 = 18 \text{ km/h}$$

$$30 \text{ km/h}$$

$$180 \text{ km/h}$$

$$\text{Speed} = 180 + 30 = 210$$

192 km/h
 Choro



**Next Class se Hoga
Level Up..**

